



HAL
open science

A Latent Heat Storage System for Low-Temperature Applications: From Materials Selection to Prototype Performances

Didier Haillot, Yasmine Lalau, Erwin Franquet, Sacha Rigal, Frederic Jay,
Jean-Pierre Bedecarrats

► To cite this version:

Didier Haillot, Yasmine Lalau, Erwin Franquet, Sacha Rigal, Frederic Jay, et al.. A Latent Heat Storage System for Low-Temperature Applications: From Materials Selection to Prototype Performances. Applied Sciences, 2021, 11 (21), pp.10350. 10.3390/app112110350 . hal-03414930

HAL Id: hal-03414930

<https://imt-mines-albi.hal.science/hal-03414930v1>

Submitted on 5 Nov 2021

HAL is a multi-disciplinary open access archive for the deposit and dissemination of scientific research documents, whether they are published or not. The documents may come from teaching and research institutions in France or abroad, or from public or private research centers.

L'archive ouverte pluridisciplinaire **HAL**, est destinée au dépôt et à la diffusion de documents scientifiques de niveau recherche, publiés ou non, émanant des établissements d'enseignement et de recherche français ou étrangers, des laboratoires publics ou privés.



Distributed under a Creative Commons Attribution 4.0 International License

Article

A Latent Heat Storage System for Low-Temperature Applications: From Materials Selection to Prototype Performances

Didier Haillot ^{1,2,*}, Yasmine Lalau ^{2,3}, Erwin Franquet ^{2,4}, Sacha Rigal ², Frederic Jay ⁵
and Jean-Pierre Bédécarrats ²¹ Mechanical Engineering Department, École de Technologie Supérieure, Montréal, QC H3C1K3, Canada² Université de Pau et des Pays de l'Adour, E2S UPPA, LaTEP, Laboratoire de Thermique, Énergétique et Procédés, 64000 Pau, France; yasmine.lalau@mines-albi.fr (Y.L.); erwin.franquet@univ-cotedazur.fr (E.F.); sachar.rigal@outlook.com (S.R.); jean-pierre.bedecarrats@univ-pau.fr (J.-P.B.)³ Université de Toulouse, Mines Albi, CNRS, Centre RAPSODEE, Campus Jarlard, CEDEX 09, 81013 Albi, France⁴ Polytech'Lab, University Côte d'Azur, 06200 Nice, France⁵ Carrier, Propriétaire de la Marque Commerciale CRISTOPIA, 78 ch. du Moulin de la Clue, 06140 Vence, France; frederic.jay@carrier.com

* Correspondence: didier.haillot@etsmtl.ca

Abstract: The industrial sector is increasingly obliged to reduce its energy consumption and greenhouse gases emissions to contribute to the world organizations' targets in energy transition. An energy efficiency solution lies in the development of thermal energy storage systems, which are notably lacking in the low-temperature range (50–85 °C), for applications such as district heating or low-temperature waste heat recovery. This work aims to bring a latent heat storage solution from material selection to prototype evaluation. The first part of this paper is dedicated to the characterization and aging of a phase change material selected from a screening of the literature (fatty acid mixture mainly composed by stearic and palmitic acid). Then, this material is encapsulated and tested in a prototype whose performances are evaluated under various operating conditions. Finally, a numerical model validated by the experimental results is used to explore the influence of a wider range of operating conditions, dimensioning choices, and material conductivity improvements.

Keywords: latent thermal energy storage; phase change material; calorimetry; thermogravimetry; experimental studies; numerical model



Citation: Haillot, D.; Lalau, Y.; Franquet, E.; Rigal, S.; Jay, F.; Bédécarrats, J.-P. A Latent Heat Storage System for Low-Temperature Applications: From Materials Selection to Prototype Performances. *Appl. Sci.* **2021**, *11*, 10350. <https://doi.org/10.3390/app112110350>

Academic Editor: Adrián Mota Babiloni

Received: 21 September 2021

Accepted: 27 October 2021

Published: 4 November 2021

Publisher's Note: MDPI stays neutral with regard to jurisdictional claims in published maps and institutional affiliations.



Copyright: © 2021 by the authors. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (<https://creativecommons.org/licenses/by/4.0/>).

1. Introduction

In the current environmental and energy context, the industrial sector is being forced to reduce its energy consumption. This involves improving the energy efficiency of its systems [1]. Indeed, energy efficiency is one of the pillars of the EU's Energy Union strategy and has been proposed as a highly effective way to lower emissions, reduce energy dependency, and increase security of supply. Thanks to a Thermal Energy Storage (TES) system, the production and consumption of energy can be decoupled, as this is a powerful tool to optimize energy efficiency, valorizing energy that would otherwise be wasted. For these reasons, TES systems have received growing attention in recent years, as shown by Alva et al., whose review presents most of the applications, advances and scientific and technological challenges of this technology [2]. Combining high storage capacities and possible energy restitution at almost constant temperature, the solution of TES using phase change materials, called PCMs, appears as a particularly attractive solution. However, the current implementation of these storage systems comes up against scientific and technological obstacles, regarding both the storage material and the system, but also as to its integration and management in industrial processes [3].

To tackle these challenges, a collaborative project aiming at developing a solid–liquid PCM TES system has been carried out. The temperature range targeted is between 50 and 85 °C, and so this can be considered as a low-temperature TES system. Typical end uses in this temperature range are district heating systems [4,5], domestic heating systems [6], or low-temperature waste heat recovery for industry [7], including in mobile applications [8]. Each TES is composed of a “storage material”, in our case a PCM, integrated into a “system”, and it can be interfaced with one or more applications using a heat transfer fluid (HTF). To integrate the TES in these applications, an envelope ensuring the interface between the HTF and the PCM must be designed. This envelope should show good thermal stability, corrosion resistance and mechanical resistance; guarantee an effective barrier while optimizing the heat transfer between the PCM and the HTF; allow easy implementation [9]. Two routes are usually chosen: PCM addition to a jacketed heat exchanger [10] or PCM encapsulation in spherical, cylindrical [11] or parallelepipedal [12] containers. The encapsulation technique is employed at the industrial scale [13–15], and even at the micro-scale level [16], and has been chosen for this project. The selected storage process consists of filling a cylindrical tank with plastic capsules that contain the PCM. An HTF flows through the tank and around the capsules at a low velocity. During the charge mode, the temperature of the HTF is higher than the melting temperature of the PCM, causing the encapsulated PCM to melt. To discharge the heat from the storage, the cold fluid coming from the load receives energy from the capsules, causing the PCM to crystallize. Once this design has been selected, some questions and technological barriers are still present at different levels.

First, regarding the materials, various PCMs applicable in this range of temperature (50–85 °C) are already known [17]. Based on a previous literature screening [18–20] and on technical requirements, an industrial-grade fatty acid mixture was selected. Indeed, both its melting temperature and its volume storage capacity enthalpy are in the targeted range. Furthermore, this material is not corrosive, nor is it flammable or toxic to humans and/or the environment. Finally, it is available in industrial quantities and its cost per kilogram does not exceed the price of EUR 5/kg to fulfil the industrial partner’s requirement. While the thermo-physical properties of pure or binary fatty acids are well-known, data regarding industrial-grade mixtures, especially aging and compatibility with the encapsulation material, are still missing.

Second, the PCM’s behavior should be studied while it is being implemented in a storage system to fulfill a technological scale-up. In the focused temperature range, some laboratory-scale experiments have been conducted in the context of encapsulated PCM for exhaust gas heat recovery [21] or tubular heat exchange for domestic hot water supply [22]. However, both the PCM and encapsulation material in these processes are different from those in this project. A set-up has to be built to study the specific experimental configurations of interest.

Third, those experimental works can demonstrate the technical solutions’ feasibility and provide information on their behavior at the system level. However, the extended investigation of the influence of variations in the operating conditions or dimensioning choices must be approached by a numerical model.

The following paper is divided into three parts that deal with the three aforementioned issues: PCM characterization and aging related to its use conditions; the system performance assessment through prototype development and running; parametric study by a numerical model of the operating conditions and sizing choices.

2. Calorimetric Analysis, Aging and Compatibility Studies on Industrial-Grade Fatty Acid Mixture

The PCM was supplied by the chemical product trading company Altichem[®]. This product is an industrial-grade mixture of different fatty acids in the proportions listed in Table 1, mainly stearic acid and palmitic acid.

Table 1. Composition of the industrial grade fatty acid mixture.

Compound	Formula	Mass Percentage (%)
Stearic acid	CH ₃ (CH ₂) ₁₆ COOH	50–55
Palmitic acid	CH ₃ (CH ₂) ₁₄ COOH	42–50
Myristic acid	CH ₃ (CH ₂) ₁₂ COOH	0–2
Lauric acid	CH ₃ (CH ₂) ₁₀ COOH	0–1
Others		0–1.5

Stearic acid (SA) or octadecanoic acid, CH₃(CH₂)₁₆COOH, is a fatty acid with interesting chemical characteristics (non-toxic, non-corrosive, MSDS with only one symbol: Xn). It is a white to yellowish-white amorphous waxy solid, with a tallow-like odor and taste, that is very slightly soluble in water but soluble in alcohol, ether and acetone. It is a combustible when exposed to heat or flame. Palmitic acid (PA) or hexadecanoic acid, CH₃(CH₂)₁₄COOH, has the same characteristics. PA is naturally present in palm oil and various animals or plants, and widely used in the food industry and soap fabrication. SA is used in a wide range of applications, such as in candles; in chemicals; in dispersants; as a softener in rubber compounds, food packaging and PVC lubricant; a direct food additive; a clarifying agent (wine); a textile auxiliary; an intermediate for paints; an emollient/superfating agent in cosmetics; a paper sizing ingredient; a masticatory substance in chewing gum; in pharmaceuticals [23]. SA's latent heat of fusion is equal to 200 J/g and its density is 940 kg/m³, thus, its volume storage capacity is about 52 kWh/m³ [24]. This value is quite close to that of PA, 51.5 kWh/m³, with a latent heat of fusion equal to 206 J/g and a density of 900 kg/m³ [25]. Their melting temperatures are respectively 70 and 63 °C.

Although the properties of pure or binary fatty acid are well documented [25], data regarding their industrial-grade use are missing, and a complete experimental characterization of the PCM mixture must be performed. Furthermore, the stability of the key thermo-physical properties over thermal cycling and extended temperature exposure periods must be studied.

Moreover, as the encapsulation technique has been chosen to ensure the interface between the HTF and the PCM in the TES system, the design of the test bench (Section 3) will include spherical polyolefin capsules filled with the PCM mixture. These capsules, provided by the industrial partner, are called nodules and are made of polyolefin (outer diameter 98 mm, width 2 mm). Thermal characterization, aging and compatibility studies of the industrial-grade SA–PA mixture with these nodules are thus necessary.

2.1. Experimental Procedure

Two measurement devices were used: the differential scanning calorimetry (DSC) technique and thermogravimetric (TD) analysis.

The DSC technique is used to validate the basic parameters of the PCMs, namely, their melting temperature (T_{mp}) and enthalpy variation (L) during phase change. The melting point temperature is approximated by the onset technique if the PCM is pure, but if mixtures are analyzed, this onset refers only to the beginning of the transition. The latent heat is determined from the integration of the heat flow signal over the transition period [26]. Both these steps were undertaken using the Setaram DSC131 in 120 µL cells. A melting/crystallization cycle is carried out at a heating rate of 2 °C/min, limiting the cells' inner thermal gradients.

The stability of the PCM over thermal cycles is then characterized using the same technique but on a different equipment (Perkin-Elmer Pyris Diamond), reducing the experiment time as it works with higher heating rates (20 °C/min), thanks to a small crucible (60 µL) and a power compensation system.

Both measurements follow a similar temperature scan protocol, involving at least three melting/crystallization cycles around the melting temperature (+/−35 and 30 °C, respectively, for the parameters' validation and the stability study), each cycle being separated by an isothermal *plateau* ensuring a complete phase change (5 min for the

Setaram DSC131 and 1 min for the Perkin Elmer Pyris Diamond). The first thermal cycle melts the PCM and generates its homogeneous distribution at the bottom of the crucible to optimize its thermal contact with the walls. The second cycle, called the reference cycle, is used to measure the temperature and the change in enthalpy during the phase transition. Finally, the third cycle is used to check the thermo-physical properties measured during the second cycle. That third cycle is then compared to the 38th and 75th cycles in the case of the stability study.

The cell and sample masses were weighted before and after the DSC measurement using a Mettler Toledo XP26 (uncertainty ± 0.002 mg). Additionally, the two calorimeters were calibrated, for temperature and energy, using five standard materials whose properties are referenced in Table 2.

Table 2. Standard calibration substances used.

Compound	T_{mp} (°C)	L (J/g)	Purity (%)
Gallium	29.76	80.17	99.99999
Naphthalene	80.23	148.11	99.9
Benzoic acid	122.35	147.9	100
Indium	156.60	28.45	99.99
Tin	231.88	60.46	99.9985

Measurement uncertainties due to environmental conditions (temperature and humidity variations) and experimental conditions (related to the measuring devices during filling, packaging and weighting of the crucibles in the first instance, and then to the post-processing of the results in the second instance) were estimated via a repeatability study on a standard substance whose melting temperature is closest to our field of study, i.e., Naphthalene. Five strictly identical experiments were performed on each calorimeter to determine the standard deviation (σ) of the T_{mp} and L distribution. The uncertainty (δ) was then provided by Student's Law (Equation (1)), which is particularly suitable when the number of experiments is small.

$$\delta = St_{N-1,\gamma} \cdot \frac{\sigma}{\sqrt{N}} \quad (1)$$

$St_{N-1,\gamma}$ is Student's number, which depends on the number of experiments and the level of confidence, γ , desired (in our case $N = 5$ and $\gamma = 99\%$, thus $St_{4,99\%} = 4.604$). The application of this method to the Setaram DSC131 apparatus leads us to consider an uncertainty of ± 0.2 °C on the melting temperature and $\pm 4.9\%$ on the latent heat. As for the Perkin Elmer Pyris Diamond DSC, given our experimental conditions, with higher heating rates, these uncertainties are respectively ± 0.5 °C and $\pm 1.3\%$.

The TG analysis is used to observe the PCM mixture's mass variations when it is subjected to a temperature rise in a controlled atmosphere. A mass loss above 1% of the initial mass would reveal a thermal degradation. The experiment is performed with Setaram SETSYS apparatus and begins with an isothermal *plateau* imposed at 20 °C. Then the temperature is raised at 2 °C/min up to 150 °C. The chosen carrier gas is air in respect to the technological target of this research work and the complications of conditioning a PCM within a spherical capsule under an inert atmosphere.

2.2. Thermal Characterization of Stearic Acid–Palmitic Acid Mixture

Figure 1 presents results of the thermal analysis of the SA–PA mixture. Figure 1a shows the result of DSC in dynamic mode using the Setaram DSC131. The mixture showed no supercooling issue for a sample mass of 32.324 ± 0.004 mg. The melting onset temperature was measured at 53.8 ± 0.2 °C, and the change in enthalpy of fusion was estimated at 178 ± 9 J/g, i.e., 47.3 kWh/m³. Those properties are equal to those measured by [27] for a similar industrial fatty acid mixture, and close to the industrial-grade pure stearic acid studied by [28].

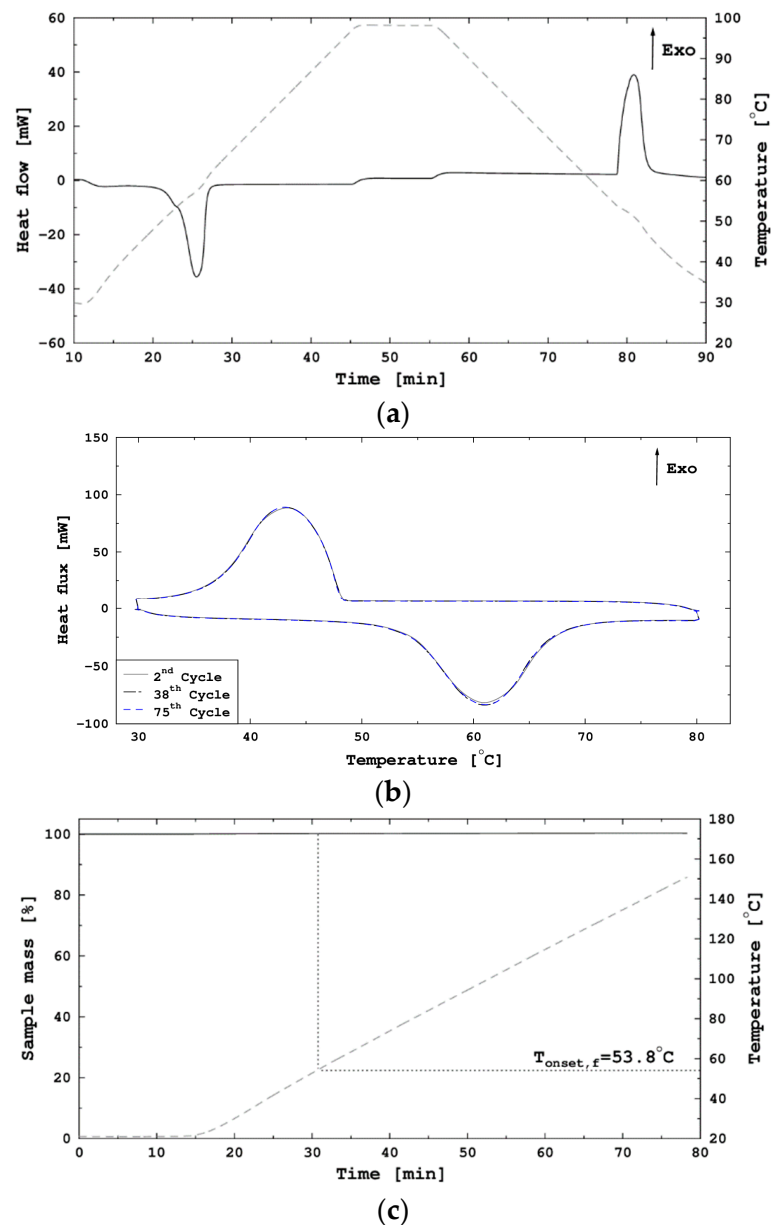


Figure 1. SA–PA mixture thermal analysis: (a) DSC determination of transition temperature and enthalpy (Setaram DSC131, sample mass 32.324 ± 0.004 mg), (b) DSC cycling (Perkin-Elmer Pyris Diamond, sample mass 11.080 ± 0.004 mg) and (c) TG analysis (Setaram SETSYS).

Figure 1b presents the results of thermal cycling using the Perkin Elmer Pyris Diamond DSC with the superposition of the 2nd, 38th and 75th cycles of the SA–PA mixture. The mass of the sample is then 11.080 ± 0.004 mg. The results indicate that this PCM keeps its thermo-physical properties during thermal cycling as the 2nd, 38th and 75th cycle thermograms are strictly similar.

Figure 1c shows the thermogravimetric analysis of the SA–PA mixture (Setaram SETSYS apparatus). The melting onset temperature is plotted on the graph (53.8°C). It can be noted that up to the final temperature of the experiment, i.e., 150°C , no mass loss is evident.

2.3. Aging of SA–PA Mixture

The SA–PA mixture's thermal stability was assessed through long-term exposure to temperatures above its melting temperature, at levels that could be encountered in an

industrial context. PCM samples in hermetically sealed flasks were put in three stoves and monitored at the following temperatures: 65 °C, 75 °C and 85 °C. The properties were examined after 7, 14, 21 and 28 days, each measurement being conducted on a dedicated flask to avoid sample pollution. The standard operating conditions involve stability at 10 °C above the melting temperature, while isolated monitoring accidents could expose the PCM at higher temperatures for shorter periods. Those accidental exposure durations are difficult to predict, but as an order of magnitude, a 20 min exposure per week would lead to approximately 15 days of high-temperature exposure throughout the 20 years of a system's lifetime. The aging studies were then conducted using such durations.

As a first step, a visual check of the samples in the oven was carried out to highlight the possible impact of the temperature and duration of the experiment on the PCM. Regardless of the temperature to which the sample was subjected, no degradation of the material could be visually observed.

The second step consisted of a calorimetric analysis of the sample with Setaram DSC 131 following the protocol detailed in paragraph 2.1. The results, presented in Figure 2, show the evolution of key thermo-physical properties as a function of exposure time at the selected temperatures: 65 °C (black line with circles), 75 °C (gray dotted line with squares) and 85 °C (blue dotted line with triangles). Uncertainty has also been added to the graph.

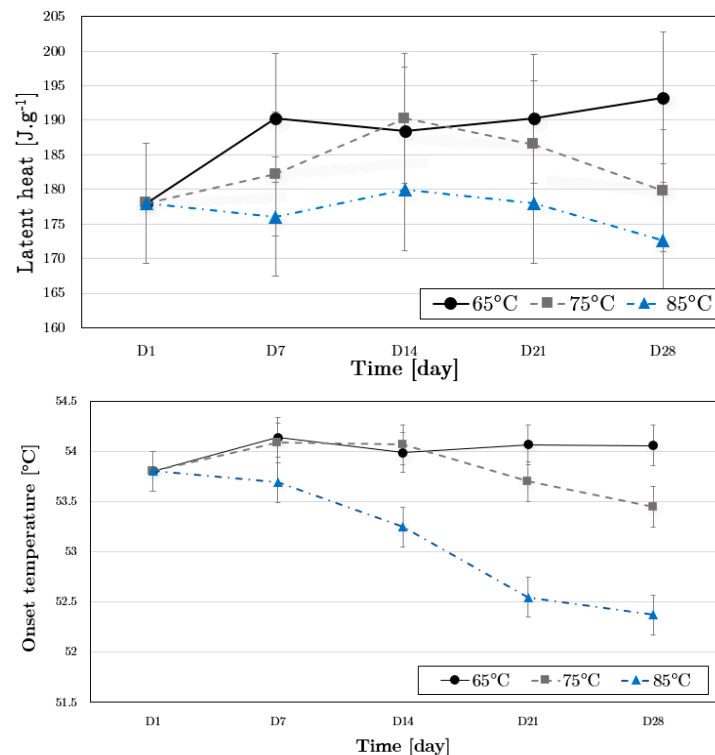


Figure 2. SA-PA mixture properties' evolution over constant temperature exposure: latent heat of fusion (**top**) and onset temperature (**bottom**).

A disparity in latent heat values between the three temperatures is visible in Figure 2 after seven days, with 190 J/g for the sample placed at 65 °C, 182 J/g for the sample placed at 75 °C and 176 J/g for the sample placed at 85 °C. However, this difference remains at a value within the error interval throughout its thermal exposure, at all studied temperature levels. On the contrary, regarding the graph presenting the onset temperature as a function of time, differences are more noticeable between the samples. If the melting onset temperatures of the PCM placed at 65 °C and 75 °C are constant over time, the samples subjected to a temperature of 85 °C show a reduction of almost 2 °C between the reference time (D1), where the PCM is unaged, and the 28th day (D28).

Thus, the SA–PA mixture has a satisfying thermal stability when used up to 75 °C, but the operating conditions should avoid prolonged use at 85 °C and above, in order to maintain the initial melting onset temperature.

2.4. Compatibility between the PCM and Its Capsule

The second part of this aging study aims to conclude whether the encapsulation significantly alters the thermo-physical properties of the SA–PA mixture. In other words, it is important to know if contact between the polyolefin mixture (polyethylene and polypropylene) constituting the spherical capsules (nodules) and the SA–PA mixture induces significant differences in the latter's storage capacities. Compatibility tests were carried out in the same ovens as the aging tests, i.e., at a fixed temperature, and the time and temperature constraints were also similar. Nodule pieces were sliced and then inserted into the flasks and completely immersed in the PCM. As many flasks as the number of samples needed for analysis were prepared. At the end of the experiment, the flasks were removed from the oven, photographed, and weighed. A sample of PCM was taken for analysis, then the nodule piece was removed from the bottle and photographed. A thorough study of the condition of the nodule would require additional investigations, such as tensile tests, to analyze the evolution of the material's resistance over time according to the working temperature. However, as such analysis was not covered in the frame of this project, only visual and mass observations of the nodule were carried out.

Figure 3 shows an example of the evolution of the visual appearance of the nodule pieces inserted within the flasks containing the SA–PA mixture. Photographs were taken of nodule pieces from flasks placed at 85 °C, the highest temperature stress, and removed after 7 days and then 28 days.



Figure 3. Nodule pieces after 7 days (**left**) and 28 days (**right**) in contact with the SA–PA mixture at 85 °C.

The two nodule pieces showed no visual changes, and therefore do not appear to have been degraded by contact with stearic acid over time. Their irregular shape is due to the fact that they were cut from a spherical nodule, and not to their undergoing plastic deformation due to exposure to high temperatures.

Figure 4 shows the evolution of the latent heat of fusion and onset temperature of the SA–PA mixture as a function of storage time and temperature.

The same behavior was observed whether the SA–PA mixture was or was not in contact with a sample of the nodule; that is, the latent heat was stable over the experiment time whatever the temperature, and a decrease in the onset temperature was recorded at 85 °C.

No compatibility issue was detected between the SA–PA and the encapsulation material. However, a compatibility study on pure stearic and palmitic acid and various plastics, including polypropylene, underlined the plastic swelling issue, possibly leading to its mechanical resistance degradation [25]. Some caution should then be taken when conducting the experimental campaign on the prototype, monitoring the nodules' integrity.

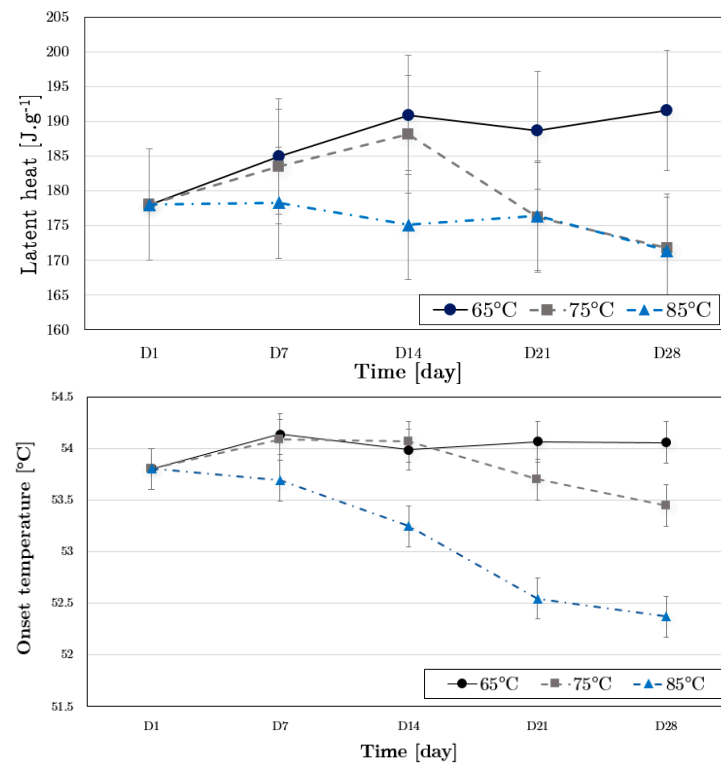


Figure 4. SA–PA mixture’s properties’ evolution over constant temperature exposure and in contact with polyolefin sample: latent heat of fusion (**top**) and onset temperature (**bottom**).

3. Experimental TES System: Design, Construction, and Performance Evaluation of a Prototype

3.1. Development of a TES Test Bench

A prototype of a TES system has been built in the LaTEP laboratory and is presented in Figure 5. It is composed of a 0.1 m³ cylindrical tank (0.4 m diameter and 0.8 m length) made of steel and filled with spherical nodules that contain the SA–PA mixture studied in the previous paragraph. Water is used as the HTF. The tank can rotate around a horizontal axis so the test can be performed in vertical or horizontal positions.

For efficient storage, it is important to respect the natural thermal stratification of the HTF inside the tank during the charge and discharge modes. During the phase change, additional natural convection movements of the HTF occur near the nodule due to PCM latent heat. When the forced circulation of the HTF (due to the pump) is in the same direction as these natural convection movements, then the storage (or discharge) process is efficient. Thus, when the tank is in a vertical position, the HTF flows through the tank from top to bottom for the charge (heating) mode and from bottom to top for the discharge (cooling) mode. When the tank is in a horizontal position, a specific diffuser allows the HTF to flow vertically through the tank.

The spherical capsules have an external diameter of 98 mm and are blow-molded from a blend of polyolefins with an average thickness of 2 mm. They are partially filled with the SA–PA mixture, leaving an empty volume, making thermal expansion possible when the PCM melts. To measure the spatial–temporal evolution of the temperature, several T-type thermocouples (wire diameter 0.5 mm) are located at different places inside the tank. They are set on bars fixed on the vertical axial bar. Note that these thermocouples measure the local temperature of the HTF. Moreover, a thermocouple is fixed on the external surfaces of eight capsules by means of a steel ring. These thermocouples allow one to detect the instant and the duration of the crystallization. In this experimental configuration, the tank contains 84 capsules totaling 32.5 kg of SA–PA mixture, but can receive up to 121 capsules by removing part of the instrumentation. As the thermocouples are connected to a data

acquisition system (CompactDAQ cDAQ-9188—National Instruments), it is possible to determine the temperature with a precision of 0.5 K at different points inside the tank, located in relation to radius and the height, versus time. The properties and geometric data are referenced in Tables 3 and 4. The tank is insulated with glass wool. The HTF flow rate is measured by a Coriolis flowmeter (CMF100 from MICRO MOTION ELITE, 1% error).

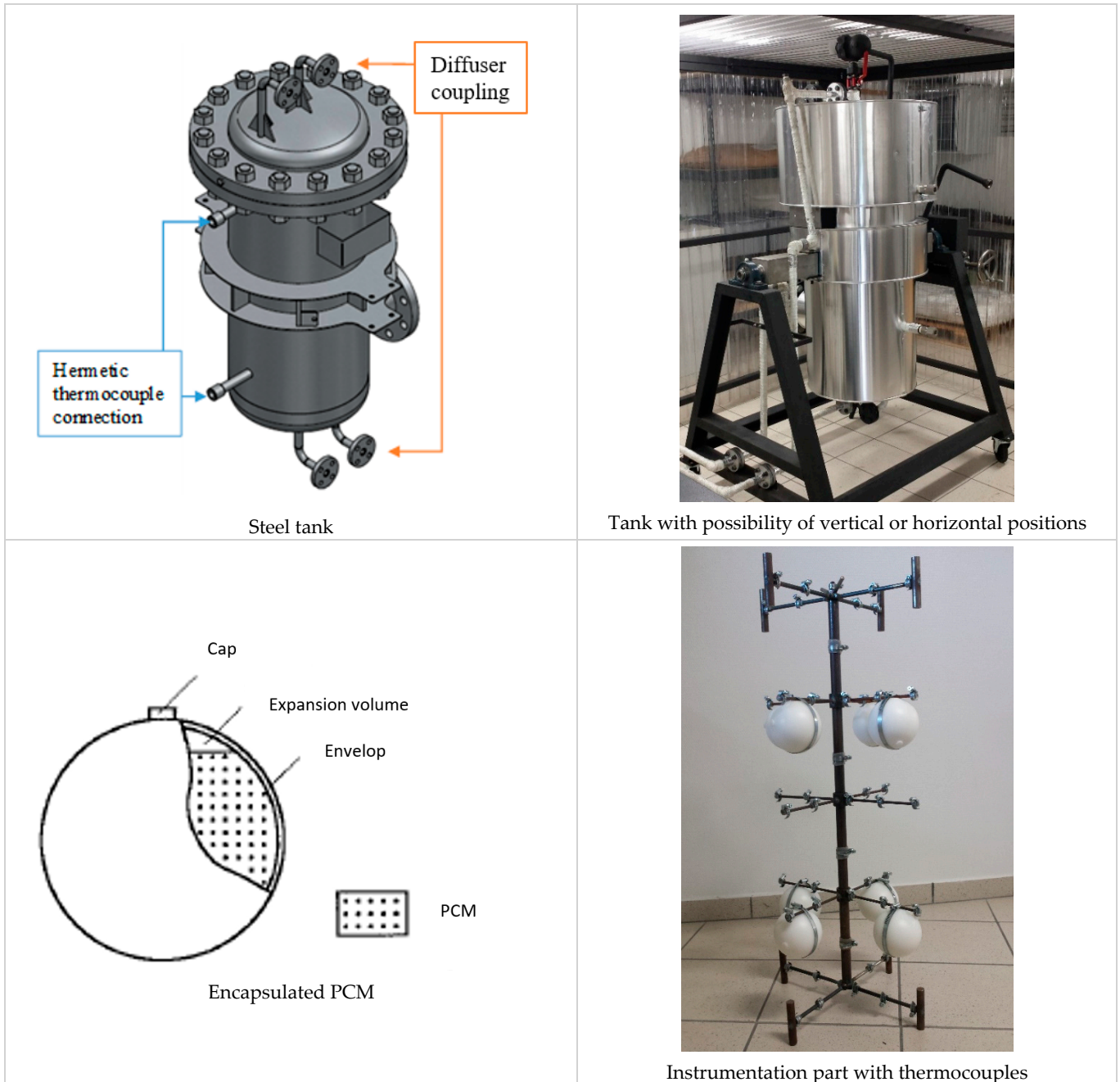


Figure 5. Laboratory-scale latent TES prototype.

Table 3. Materials' thermo-physical properties.

Materials	λ (W/m·K)	ρ (kg/m ³)	C_p (J/kg·K)
Water (HTF)	0.6	986	4182
PCM	0.176 (sol.)–0.172 (liqu.)	940	2300 *
Steel (tank)	50.2	7850	473
Polyolefin (Nodules)	0.41	905	1900
Glass wool (insulation)	0.035	na	na

* [29,30].

Table 4. System geometry.

Material	Thickness (m)	Outer Diameter (m)	Length (m)
Tank	0.004	0.4	0.8
Nodules	0.002	0.098	na
Insulation	0.05	na	na

3.2. Experimental Results and Discussion

More than thirty charges and discharges have been performed on the lab scale prototype. During tests, no degradation of the system's performance was observed. Figure 6 describes the results for a storage phase. The tank was set in the vertical position and the HTF flowed from the top to the bottom of the tank. The HTF was heated at a constant rate up to a temperature at which it was then maintained afterwards. The temperatures are presented for an experiment performed at a heating rate of 2 °C/h, a final temperature of 64.6 °C and a volume flow rate of 100 L/h. This highlights that the temperatures in the cylindrical tank were symmetrical and independent of the radius (Figure 6a). Furthermore, as illustrated in Figure 6b, the storage prototype worked perfectly as a piston-type system i.e., the temperature was constant on a section perpendicular to the fluid flow.

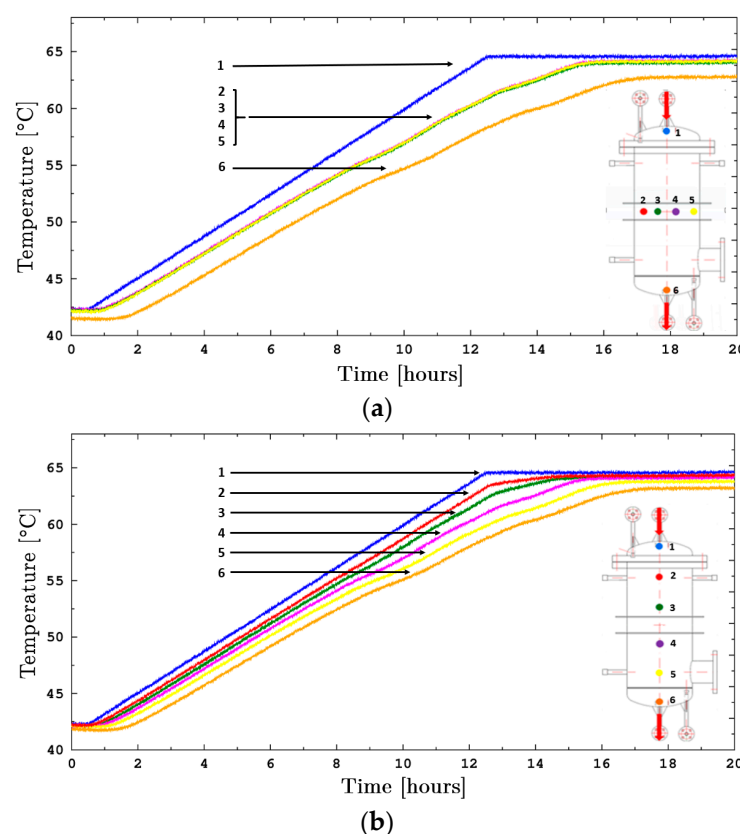


Figure 6. Evolution of temperatures vs. time for a charge between 42.3 °C and 64.6 °C at 100 L/h. (a) Horizontal temperature variation, (b) vertical temperature variation.

The outlet temperature of the tank started to increase almost 2 h after the inlet temperature had increased, which corresponds to the time it takes for the HTF to cross the tank. The stored heat was mainly in the form of sensible heat up until ~8h. After that, the phase change of the SA–PA mixture began, resulting in the change in slope of the temperature curves in the tank due to the latent heat. This is particularly visible in the curves recorded in the bottom of the tank. When all the PCM mixture had melted, the storage became sensible again (liquid phase) and the outlet temperature quickly reached its final value (lower than the inlet because of the prototype's thermal losses). A similar behavior was observed during the discharge (cooling mode—see Figure 8). In both figures, the change in slope is not very large because the value of the latent heat of the PCM was quite low versus the sensible heat. This is due to the small volume of PCM that was inside the tank. The main reason is the instrumentation inside the tank, which severely reduce the space available for nodules.

3.2.1. Analytic System Description

To assess the TES system's performance, the stored energy (latent E_L and sensible E_S) are determined with Equation (2).

$$E_{stored} = E_L + E_S = m_{PCM} \cdot \Delta H_m + \int_{T_i}^{T_m} m_{PCM} \cdot C_{p_s} \cdot dT + \int_{T_m}^{T_f} m_{PCM} \cdot C_{p_l} \cdot dT + \sum_j \int_{T_i}^{T_f} m_j \cdot C_{p_j} \cdot dT \quad (2)$$

with m_{PCM} as the total PCM mass in the tank and ΔH_m its enthalpy of fusion. C_{p_s} and C_{p_l} are respectively the solid and liquid PCM heat capacity; m_j and C_{p_j} stand for the total mass and heat capacity of the remaining storage components (plastic capsules, steel tank and water HTF). T_i and T_f are the initial and final temperatures.

The efficiency is obtained with Equation (3).

$$\eta_{stored/discharged} = \frac{E_{stored/discharged}}{E_{provided}} = \frac{E_L + E_S}{E_L + E_S + E_{losses}} \times 100 \quad (3)$$

where the energy losses E_{losses} were determined as a function of the tank temperature from previous experiments performed under steady-state conditions at different temperature levels. The time needed to reach a fully charged state, $\tau_{95\%}$, is defined when the stored energy is equal to 95% of its final value, reached at the end of the experiment. In the experiment previously presented in Figure 6, 4.4 kWh was stored (1.4 kWh of latent heat and 3 kWh of sensible heat), and 2.6 kWh was lost. While the HTF introduced 7.2 kWh of heat to the tank during this experiment, the energy balance deviation was about 3%. While the uncertainty on the thermocouple could rise by 10%, a deviation below this value is acceptable. Compared to a tank filled only with water, the storage energy density is increased by 26%, but should be about 34% without measurement instrumentation. Besides this, the thermal insulation could be improved (several thermal bridges were observed), together increasing the system efficiency, which was only $\eta_{stored} = 63\%$ in the experiment presented in Figure 6.

3.2.2. Impact of the Operating Conditions

Different experiments have been performed to highlight the influence of the HTF flowrate \dot{m}_{HTF} and inlet temperature (T_{in}) during the storage and discharge phases. The studied parameters were storage efficiency η_{stored} and responsiveness $\tau_{95\%}$. The latter is defined as the time required for the storage to reach 95% of the total charged or discharged energy. Specific results for storage phase are presented in Table 5.

Table 5. Flow rate and inlet temperature influence on the TES storage time and efficiency.

	Flow Rate Influence		Inlet Temperature Influence	
$T_{in,i}$ (°C)	43.8		44.7 °C	
$T_{in,f}$ (°C)	65.8		72.7	67.9
\dot{m}_{HTF} (L/h)	626	353	288	
E_{stored} (kWh)	4.2	4.1	5.0	4.4
E_{losses} (kWh)	0.8	0.9	0.6	0.8
$\tau_{95\%}$ (h)	3.0	3.5	1.9	2.5
η_{stored} (%)	84	82	89	85

Table 5 highlights that the more the flow rate increases, the faster the charge is, allowing a higher efficiency by reducing the experimental duration and thus the thermal losses. However, this increase is not proportional, since, above a certain threshold, the limitation to the thermal transfer is no longer linked to the HTF, but to the kinetics of the melting of the PCM storage material. Indeed, the investigated conditions led to a 14% gain in charge duration by doubling the mass flowrate. The inlet temperature's increase was more efficient in reducing the storage duration: a 24% reduction was reached by a 5 °C increase, which is acceptable regarding the PCM thermal aging behavior presented in Section 2. The study of the tank in two positions, vertical and horizontal, showed similar results in both cases when suitable diffusers were associated with each of these configurations.

Finally, it can be noted that after numerous hours of operation and cycling, no visible degradation was observed on the nodules, supporting suitable compatibility with the SA-PA mixture.

To explore the TES system's performance, under a broader range of operating conditions than can be experimentally addressed, a numerical model has been developed.

4. Exploring the TES Performances Improvement by a Numerical Parametric Study

The heat transfers during melting and crystallization have been widely studied [11,18,31–35], showing that the driving phenomenon is the conductive transfer during the crystallization, while natural convection may also be involved during melting. Convection modeling may be avoided by considering the effective thermal conductivity [36–38]. Based on the purely conductive heat transfer hypothesis, the resource-consumption modeling of the mobile phase change may be side-stepped by considering the enthalpy rather than the temperature in the energy conservation equation in the PCM [39–43].

At the system level, and more precisely concerning spherically encapsulated PCM systems, a review showed that despite the case studies' diversity, models based on energy conservation equations for HTF and PCM are suitable for most of the systems [44]. Due to its ease of implementation and its demonstrated viability [45], the enthalpic method is one of the more widely used [33]. Thus, it was selected for the numerical part of this study, based on a previous work [37] adapted to the particularity of the prototype presented in paragraph 3.

The aim of this numerical study is to explore the influence of monitoring parameters, materials' properties, and system size on the global system's performances. Those performances were assessed by the following parameters:

- the storage responsiveness $\tau_{95\%}$ and efficiency $\eta_{stored/discharged}$ as previously defined;
- the storage density, defined as the amount of energy stored by unit of volume;
- the valuable energy, defined as the energy discharged under industrial conditions, meaning above a temperature or power threshold.

4.1. Model Definition

The TES system is described by a C++ code, where the first law of thermodynamics is applied to the storage as an open system. Several hypotheses are considered.

First, for the HTF and the storage tank:

- the HTF is incompressible, and its flow is axial;

- the kinetic and potential energy variation are negligible;
- the thermo-physical properties are independent of the temperature;
- the tank is divided in N meshes of same size;
- the meshing is small enough to consider the temperature as uniform with one consistent mesh volume.

Second, for the PCM and the nodules:

- the PCM volume expansion during the phase change is neglected, thus the solid and liquid densities are identical, and there is no supercooling;
- the thermo-physical properties of each phase are independent of the temperature;
- the conductive heat transfer between nodules is neglected, and inside a nodule the heat transfer is only conductive;
- each tank mesh includes N_{od} nodules and each nodule includes M concentric meshes.

4.1.1. Heat Transfer Fluid (HTF)

When considering one single mesh j , the HTF internal energy variation by time step corresponds to the energy exchanged with the adjacent meshes, the nodules, and the environment (losses):

$$\rho_{HTF} \cdot V_j \cdot C_{pHTF} \cdot \frac{\partial T_j(t)}{\partial t} = \dot{m}_{HTF} \cdot C_{pHTF} \cdot [T_{j-1}(t) - T_j(t)] + \sum_{i=1}^{N_{Nod}} \phi_{i_j}(t) - \frac{[T_j(t) - T_{ext}(t)]}{R_{th,ext}} \quad (4)$$

for a tank containing N_{Nod} nodules and a HTF flowing at a mass flow \dot{m}_{HTF} with a density ρ_{HTF} and a specific heat capacity C_{pHTF} . V_j is the volume of HTF in the mesh j ; T_j and T_{j-1} are the temperature of the mesh j and $j-1$, respectively, and $\phi_{i_j}(t)$ is the heat flux exchanged between the HTF and the nodule i in the mesh j . Finally, $R_{th,ext}$ is the thermal resistance between the tank and the environment, including the conductive resistance of the steel tank and its insulation and the convective resistance from the outside ambient air. The convective heat transfer coefficient between the tank wall and the ambient air is calculated by the Churchill and Chu relation [46].

4.1.2. PCM Nodules

The heat flow $\phi_{i_j}(t)$ from the nodule i depends on the PCM state. The heat transfers inside the nodule are predicted to be purely conductive in the model, and the change of state occurs by concentric layers, starting from the nodule wall. This hypothesis is accurate during the PCM crystallization, but less valid during the melting, as the remaining solid phase will tend to fall and disturb the concentric fusion.

The heat equation inside the nodule filled with PCM is:

$$\rho_{PCM} \frac{\partial h_{PCM}}{\partial t} = \lambda_{PCM} \Delta T_{PCM} \quad (5)$$

with ρ_{PCM} the PCM density, h_{PCM} its enthalpy, λ_{PCM} its thermal conductivity and T_{PCM} its temperature.

The boundary condition is:

$$-\lambda_{PCM} S_{int,Nod} \vec{\nabla} T_{PCM}|_{R=R_{ext}} \cdot \vec{n} = h_{conv} S_{ext,Nod} (T_{w,Nod} - T_j) = \frac{T_{PCM,M} - T_j}{R_{th,Nod}} = \phi_i \quad (6)$$

where h_{conv} is the heat transfer coefficient between the HTF and the nodule wall at the temperature $T_{w,Nod}$, calculated by an empirical correlation derived from Bédécarrats et al. considering the Prandtl and Reynolds numbers, Pr and Re [37].

$$Nu = \frac{h_{conv} \cdot D_{ext}}{\lambda_{HTF}} = 1.5 \cdot Pr^{1/3} \cdot Re^{1/2} \quad (7)$$

with D_{ext} as the outer nodule's diameter and λ_{HTF} the HTF thermal conductivity.

$R_{th,Nod}$ is the thermal resistance between the PCM at a temperature $T_{PCM,M}$ and the HTF, including the nodule's conductive resistance and the fluid's convective resistance.

The PCM is considered as a pure body, its enthalpy varying with the temperature as described by Equation (8) [47]. This approach allows for fast calculation, and induces in this case a minimal variation compared to the implementation of the experimental enthalpy variation curve.

$$h(T) = \begin{cases} c_s \cdot (T - T_{ref}) + h_{ref} & T < T_m \\ c_s \cdot (T_m - T_{ref}) + \chi_l \cdot L_m + h_{ref} & T = T_m \\ c_s \cdot (T_m - T_{ref}) + L_m + c_l \cdot (T - T_m) + h_{ref} & T > T_m \end{cases} \quad (8)$$

with c_s and c_l being the specific heat capacity of the solid and liquid PCM phases, L_m its latent heat of melting and χ_l its liquid mass fraction. During the phase change, the temperature remains constant ($T = T_m$), while the liquid mass fraction varies. The reference $h_{ref} = 0$ J/kg is set at an arbitrary temperature lower than the melting temperature.

The equation is resolved by the finite element method (FEM). The model is initialized at $t = 0$ with an equal initial temperature of the PCM and the HTF. Then, at each time step, the fluid temperature and the PCM enthalpy are calculated. The mesh number N inside the tank is limited to 8 as one mesh cannot be smaller than a nodule, and the mesh number M inside a nodule is set at 24 as a compromise between accuracy and speed.

4.2. Model Validation

The experimental part of this work, presented in Section 3, has allowed the validation of the developed model via both charge and discharge operation. The inlet and outlet temperatures under the charge and discharge modes at 2 °C/h are displayed, respectively, in Figures 7 and 8, with continuous lines for the experiment and dotted lines for the numerical results. Both results follow similar evolutions, especially under the discharge mode, where the crystallization plateau is well defined. Some discrepancies appear during the charge, due to the fact that the convection phenomenon inside the nodule during the melting step is neglected in the numerical model: the melting is supposed to happen in a concentric way with conductive heat transfer, while in reality the solid core with a higher density tends towards the capsule's bottom wall, inducing convective transfers in the liquid phase. Moreover, the phase change is modeled as if the PCM were a pure body, but this is not the case for the selected SA-PA mixture.

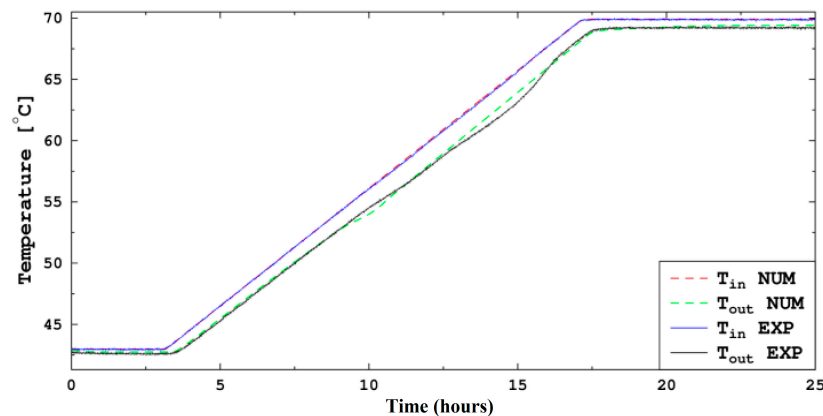


Figure 7. Charge mode from 43 to 69.9 °C at 2 °C/h and 180 L/h.

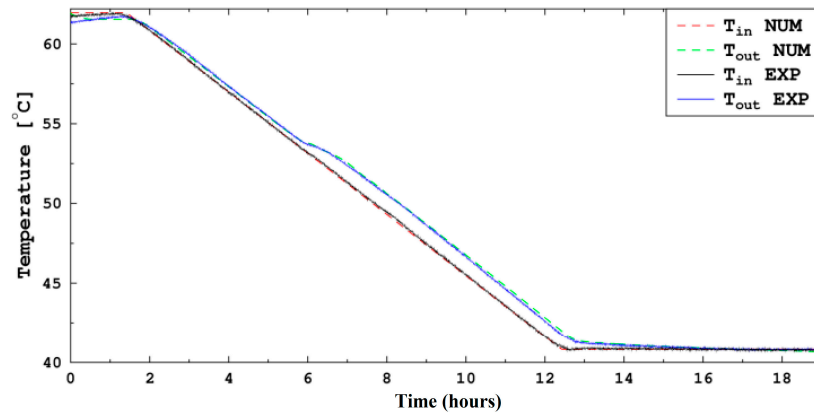


Figure 8. Discharge mode from 62.1 to 40.8 °C at 2 °C/h and 194 L/h.

The global energy balance for both experiments is synthesized in Table 6

Table 6. Energy balance—model and experiment comparison. Case study: 2 °C/h, charge 43.0–69.9 °C at 180 L/h and discharge 62.1–40.8 °C at 194 L/h.

	Charge			Discharge		
	E_{stored}	E_{losses}	Provided	$E_{discharged}$	E_{losses}	Recovered
Model	4.1 kWh	2.1 kWh	6.2 kWh	4.5 kWh	1.2 kWh	3.3 kWh
Experiment	3.9 kWh	2.5 kWh	6.4 kWh	4.1 kWh	1.2 kWh	2.9 kWh
Deviation	5.1%	16%	3.1%	9.8%	-	13.8%

With an average deviation of 8%, a maximum 16% and minimum 3.1%, the numerical model was validated and the parametric study could begin.

4.3. Temperature and Flow Rate Sensitivity Analysis

Two monitoring parameters have been explored over a larger range than the one allowed by the experimental campaign: the inlet storage temperature and the HTF mass flow rate.

The influence of the inlet temperature on the charging time, the total energy stored and the storage efficiency is depicted in Figure 9. The responsiveness decreased and the amount of energy stored increased with the inlet temperature: $\tau_{95\%}$ dropped from 7.7 h to 4.9 h and the energy stored rose from 3.5 kWh to 4.6 kWh with a respective temperature increase from 60 to 80 °C. However, the influence of the inlet temperature is less important after a certain temperature for these two parameters. The storage efficiency proportionally decreased when the inlet temperature increased, as the tank insulation was not modified, inducing higher thermal losses. Besides hits, the aging study revealed that the PCM thermo-physical properties could be damaged above 75 °C: given the decreasing gains in time and energy and the degradation risks, the most suitable inlet temperature has been defined as 70 °C.

The influence of the mass flow rate \dot{m} is shown in Figure 10.

The charging and discharging times were similarly reduced by convective heat transfer intensification due to the flow rate’s increase, with a stabilization above 0.05 kg/s. The discharge performances should also be assessed via an estimation of the valuable energy, i.e., the thermal energy available at a minimum temperature threshold. Under real operating conditions, the downstream process drives this threshold. For this parametric study, it was arbitrary set around 10 °C below the PCM melting temperature, at 45 °C. It appears that the valuable energy decreased when the flow rate increased: the convective heat transfer enhancement may be driven to a higher power but cool down faster the heat storage materials, inducing a higher proportion of thermal energy discharge at lower temperatures. The proportion of available valuable energy should be optimized by a mass flow rate adaptation during the discharge to fit with the heat demand. To pursue the

parametric study, the reference was set to a constant value of 0.05 kg/s (180 L/h), which is a compromise between the charge/discharge time and the valuable energy.

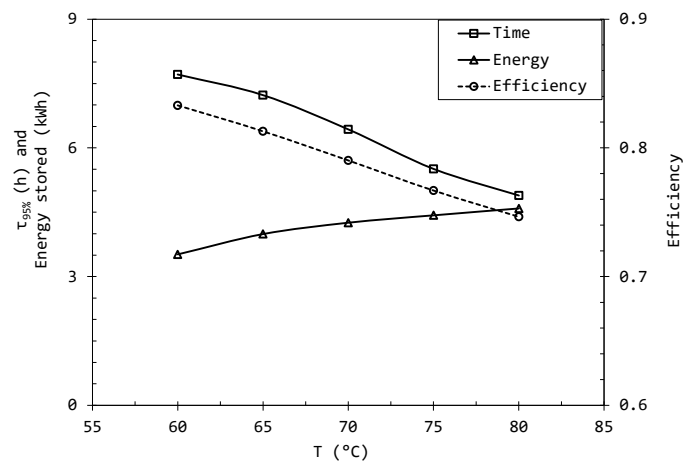


Figure 9. Charging time $\tau_{95\%}$, and energy stored (left axis) and storage efficiency (right axis), as functions of the inlet temperature during a charge from 43 °C at 0.05 kg/s.

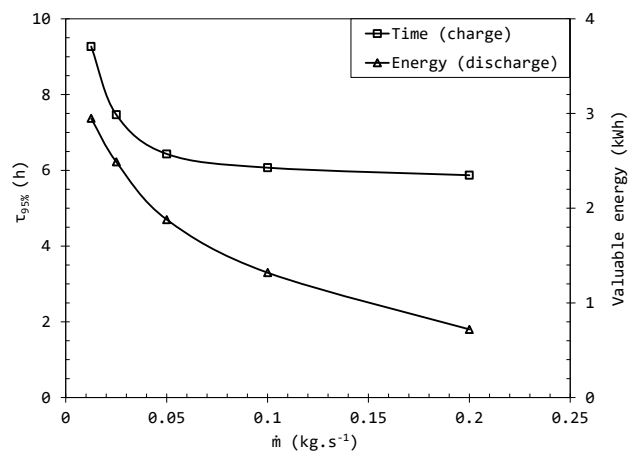
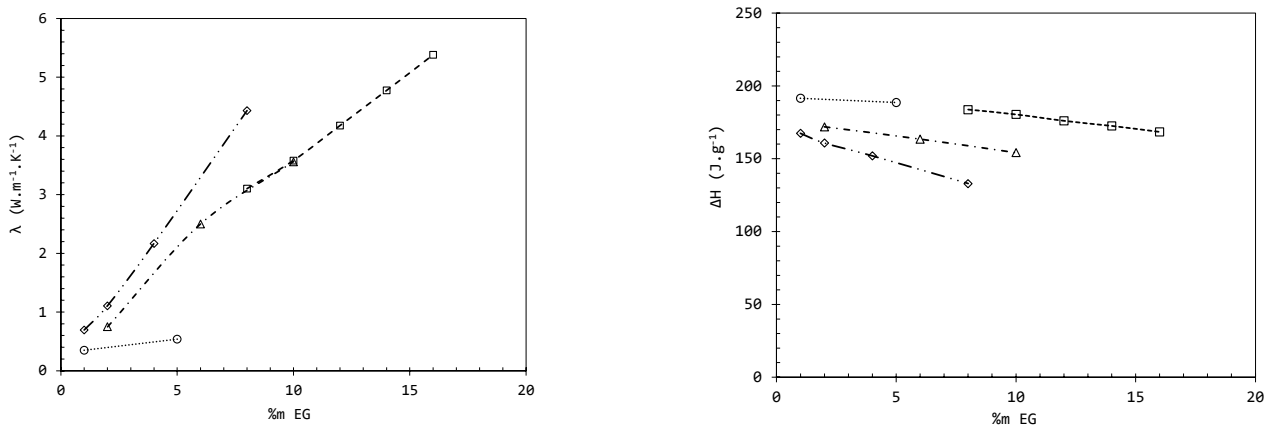


Figure 10. Charging time $\tau_{95\%}$ (left axis) and valuable discharged energy above 45 °C (right axis) as function of the mass flow rate between 43 °C and 70 °C.

4.4. Materials Conductivity Sensitivity Analysis

As previously mentioned, the reference case was a charge up to 70 °C at 0.05 kg/s (180 L/h), storing 4.4 kWh, and the targeted parameter for minimization was the charge duration $\tau_{95\%}$.

A low global thermal resistance causes the heat transfer rate to increase and $\tau_{95\%}$ to decrease. Three thermal resistances affect the storage process: convective between the HTF and the nodule, conductive in the capsule wall, and conductive in the PCM (convection in PCM is neglected). In the reference case, the two first resistances were respectively equal to 0.15 K/W and 0.06 K/W. The last one developed as the PCM melted, increasing up to 80 K/W; the limited transfer was due to the low thermal conductivity of the PCM, which is thus the main property to optimize. The PCM’s conductivity may be enhanced by various methods, a widely studied approach being loading with expanded graphite. As summarized in Figure 11, the conductivity of stearic acid-based PCM increased with the mass fraction of expanded graphite (left), while the latent heat decreased (right). Thus, a larger storage tank will be needed to store the same amount of energy, decreasing the storage energy density.



⋯○⋯Li et al. (2014) —◇—Yuan et al. (2016) -Δ- Li et al. (2019) -□- Ma et al. (2019)

Figure 11. Influence of the expanded graphite (EG) mass fraction on the PCM’s conductivity (left) and latent heat of melting (right) in the works of Li et al. (2014) [48], Yuan et al. (2016) [27], Li et al. (2019) [28] and Ma et al. (2019) [49].

The industrial-grade SA-PA mixture used to fill the prototype has similar thermo-physical properties to the one studied by [28], whose results showed intermediate values compared to the other works, and were partially repeated by [49]. Their experimental results on conductivity enhancement were then used in the following numerical results. An extrapolation was conducted, in accordance with other studies, with 28% expanded graphite to explore the effect of a conductivity value up to 50 times the standard. The heat capacity varied with the proportion of expanded graphite proportionally to its mass percentage, but the density was kept constant, as opposite influences were found in the literature [27,49].

Figure 12 scrutinizes the effects on the charging time and the system energy density (left), as well as the valuable energy available at the discharge (right). As expected, the charging time was minimized by a higher conductivity, but this improvement reached a plateau after a multiplication by ~10 of the PCM conductivity. Meanwhile, the energy density continued to decrease when expanded graphite was added: an optimum loading may be around 4%, leading to a conductivity of near 1.8 W/m·K. Besides, after this conductivity threshold, the valuable energy was no longer improved, and even started to slightly decrease after 8 W/m·K. That threshold is dependent on the system’s features, such as the HTF. For instance, in a system with air as the HTF, the convective heat transfer between the HTF and the capsule wall starts to impose limitations earlier, and it is no longer relevant to improve the conductivity of the PCM when it exceeds 1 W/m·K [50].

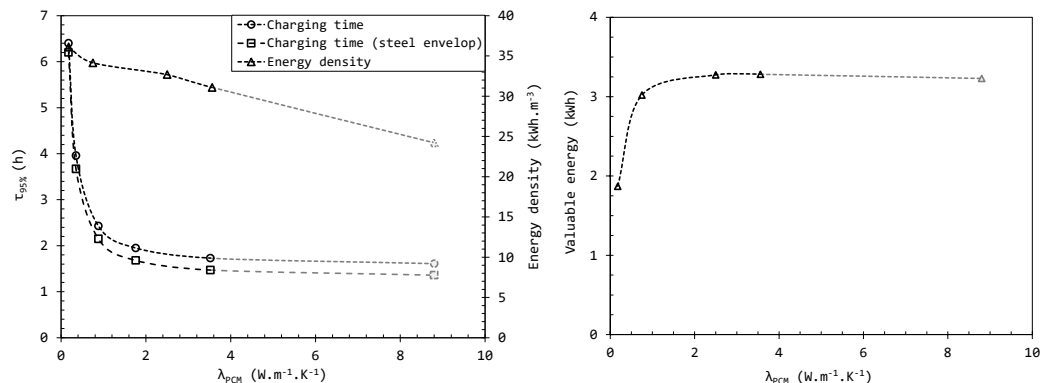


Figure 12. Charging time $\tau_{95\%}$, energy density and valuable discharge energy above 45 °C for different values of the PCM thermal conductivity.

4.5. System Sizing Sensitivity Analysis

The size of the nodules also affects the storage performance, but to a lesser extent (Figure 13). Indeed, the reduction in the diameter of the nodules from 98 mm to 77 mm (the two sizes of commercial nodules from the industrial partner's technology) made it possible to decrease the storage time by 27%. This reduction was induced by the increase by 28% in the exchange surface between the HTF and the nodules (from 3.65 m² to 4.68 m²), reducing the convective thermal resistance and consequently increasing by 26% the heat transfer between these two entities (from 228 W/m²·K to 287 W/m²·K). However, the envelop material ratio also increased, reducing the system energy density. Thus, while the charging time was reduced to ~1 h 30 with 2.5 cm-diameter nodules, the system energy density fell by 33%. This loss could be limited with thinner nodule walls (e.g., of 1 mm instead of 2 mm), but they should remain thick enough to guarantee their mechanical integrity.

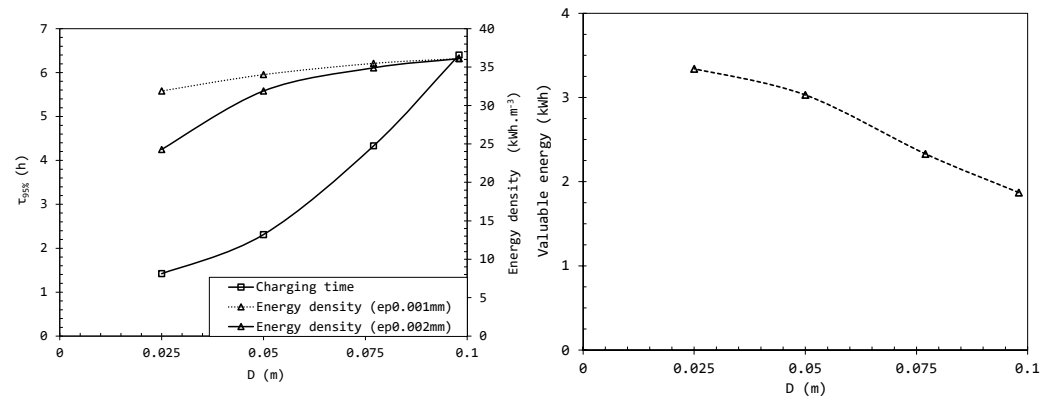


Figure 13. Influence of the nodules' diameters on the charging time $\tau_{95\%}$ (left) and valuable discharge energy above 45 °C (right).

Besides this, the quantity of valuable energy also rises when the nodules diameter is reduced, until reaching what seems to be a *plateau*. This attenuation in the rising could be even more pronounced if a full energy balance is considered, including the pumps' consumption, which would be increased by the greater pressure drop due to the smaller nodule diameters.

Finally, the influence of the dimensions of the tank was also analyzed, emphasizing the conservation of the performance of the storage with different lengths of tank and identical volumes.

5. Conclusions

The aim of this work is to develop a latent thermal energy storage system using encapsulated phase change materials (PCM) for low-temperature applications, such as district heating systems or low-temperature waste heat recovery. The objective of this paper was to investigate a suitable PCM for the TES system, to perform experimental tests on a laboratory-scale pilot to validate its use in a representative environment, and then to explore the effects of sizing and operating variations on the system's behavior via a numerical model.

The selected PCM, a stearic and palmitic acid mixture (SA-PA), was characterized by calorimetry (DSC) and thermogravimetric analysis to determine its thermo-physical properties and its thermal stability. No degradation of its thermo-physical properties was observed during the 75 successive thermal cycles, and even at 100 °C above its change-of-state temperature, the PCM did not lose 1% of its initial mass, thus showing no sign of degradation. The aging tests of PCM alone showed a conservation of the latent heat of fusion over time regardless of the chosen temperature, but a decreasing trend in the melting and crystallization onset temperatures as the exposure temperature increased. However, this decrease only appeared at a working temperature of 85 °C, which is more than 30 °C

above its change of state temperature, which is not usually reached during actual operation. Finally, the compatibility study shows that the presence of the nodule envelop in contact with this SA–PA mixture did not cause a difference in its general thermo-physical behavior: the enthalpy variations and transition temperatures during the compatibility tests were identical to those obtained during the aging tests. Considering that in both thermal aging tests, the latent heat of fusion remained stable, and the melting temperature suffered a decrease that only began with overheating to 30 °C above melting temperature, the results are considered sufficiently promising to proceed to the next step of this research project: system integration, studied through a lab prototype and a parametric numerical study.

The tests carried out on our lab-scale TES system, composed of a 0.1 m³ steel tank filled with encapsulated SA–PA mixture, are promising, despite the compactness of the nodules being reduced by almost 33% due to the metal frame supporting the thermocouples. The results also highlight the fact that the vertical or horizontal positioning of the tank does not affect the evolution of the storage process if there is a piston flow in the tank corresponding to the direction of circulation of the HTF with respect to the natural thermal stratification of the fluid. The results also show that the increase in flow rate and the difference between the inlet temperature and the melting temperature reduce the duration of the charge and discharge modes, but this reduction is limited by the PCM phase change kinetics. This storage system presents an alternative to standard hot water tanks, thanks to the larger amount of stored energy, which can rise by 34%.

Finally, the modeling of the experimental storage facility was carried out in order to simulate its thermal performance. The code was developed in C++ language, with the use of the enthalpic method, considering heat transfer in the PCM as a pure conduction problem. The temperatures provided by the model agree well with the experimental results. A slight difference is visible during the melting, and this could be caused by the fact that the natural convection phenomena within the liquid PCM are not considered. In terms of energy, the difference between the model and the experiment was less than 16%.

Various numerical studies were carried out in order to observe the influence of parameters on the TES system's performance. Increasing the flow rate, final temperature, and PCM conductivity reduces the duration of the storage. It is noted that the conductivity of the nodule envelope, due to its low thickness, has a negligible influence on storage performance. If the PCM mass is the same in the storage tank, the smaller the nodules are, the larger the exchange surface between the PCM and the HTF, and the higher the heat transfers, with a consequent decrease in storage time. Finally, a parametric study of the tank dimensions shows that the results are independent of the tank geometry if the volume is the same.

The next step of this project consists in increasing the size of the TES system and combining it with an existing industrial process. This will make the analyses of the performances of the installation possible, and determine whether the charge and discharge times are compatible. Then, an optimization study will be necessary to determine the ideal parameters of the storage facility, in order to achieve optimum performance via the targeted industrial process.

Author Contributions: Conceptualization, D.H. and J.-P.B.; software, E.F.; investigation, D.H., S.R. and Y.L.; resources, F.J.; writing—original draft preparation, D.H. and Y.L.; writing—review and editing, E.F., F.J. and J.-P.B.; supervision and funding acquisition, D.H. and J.-P.B. All authors have read and agreed to the published version of the manuscript.

Funding: This research was funded by the ANR-SEED program of the French National Research Agency (project ANR-13-SEED-0007).

Conflicts of Interest: The authors declare no conflict of interest.

Nomenclature

DSC	Differential scanning calorimetry	
HTF	Heat transfer fluid	
MSDS	Material safety data sheet	
PA	Palmitic acid	
PCM	Phase change material	
SA	Stearic acid	
TES	Thermal energy storage	
TG	Thermal gravimetric	
EU	European Union	
C_p or c	Specific heat	J/kg·K
D	Diameter	M
D1, D7, D14, D21 and D28	Days of aging test, from day 1 (D1) to day 28 (D28)	
E	Energy	J or kWh
h	Enthalpy or heat transfer coefficient	J/kg or W/m·K
L	Latent heat	J/g or kWh/m ³
m	Mass	mg or kg
\dot{m}	Mass or volume flow rate	kg/s or L/h
N	Number of experiments in Student's Law	
na	Non available	
Nu	Nusselt number	
Pr	Prandtl number	
r	Radius	M
R	Thermal resistance	K/W
Re	Reynolds number	
S	Area	m ²
$St_{N-1,\gamma}$	Student's number	
T	Temperature	°C
V	Volume	m ³
γ	Level of confidence in Student's Law	
δ	Uncertainty in Student's Law	
Δ	Variation between initial and final state	
φ	Heat transfer flux	W
λ	Thermal conductivity	W/m·K
ρ	Density	kg/m ³
η	Efficiency	
σ	Standard deviation in Student's Law	
$\tau_{95\%}$	Storage responsiveness (time to reach 95% of the final storage capacity)	hours
Subscripts		
<i>cond</i>	Conductive	
<i>conv</i>	Convective	
<i>ext</i>	External	
<i>HTF</i>	Heat transfer fluid	
<i>i</i>	Initial	
<i>in</i>	Inlet	
<i>f</i>	Final	
<i>l</i>	Liquid	
<i>L</i>	Latent	
<i>m</i>	Melting	
<i>mp</i>	Melting point	
<i>Nod</i>	Nodule	
<i>out</i>	Outlet	
<i>ref</i>	Reference	
<i>s</i>	Solid	
<i>S</i>	Sensible	
<i>th</i>	Thermal	
<i>w</i>	Wall	

References

1. Malinauskaitė, J.; Jouhara, H.; Ahmad, L.; Milani, M.; Montorsi, L.; Venturelli, M. Energy efficiency in industry: EU and national policies in Italy and the UK. *Energy* **2019**, *172*, 255–269. [CrossRef]
2. Alva, G.; Lin, Y.; Fang, G. An overview of thermal energy storage systems. *Energy* **2018**, *144*, 341–378. [CrossRef]
3. Zhang, N.; Yuan, Y.; Cao, X.; Du, Y.; Zhang, Z.; Gui, Y. Latent Heat Thermal Energy Storage Systems with Solid-Liquid Phase Change Materials: A Review. *Adv. Eng. Mater.* **2018**, *20*, 1700753. [CrossRef]
4. Lund, H.; Østergaard, P.A.; Chang, M.; Werner, S.; Svendsen, S.; Sorknæs, P.; Thorsen, J.E.; Hvelplund, F.; Mortensen, B.O.G.; Mathiesen, B.V.; et al. The status of 4th generation district heating: Research and results. *Energy* **2018**, *164*, 147–159. [CrossRef]
5. Guelpa, E.; Verda, V. Thermal energy storage in district heating and cooling systems: A review. *Appl. Energy* **2019**, *252*, 113474. [CrossRef]
6. da Cunha, J.P.; Eames, P. Compact latent heat storage decarbonisation potential for domestic hot water and space heating applications in the UK. *Appl. Therm. Eng.* **2018**, *134*, 396–406. [CrossRef]
7. Xu, Z.; Wang, R.; Yang, C. Perspectives for low-temperature waste heat recovery. *Energy* **2019**, *176*, 1037–1043. [CrossRef]
8. Du, K.; Calautit, J.; Eames, P.; Wu, Y. A state-of-the-art review of the application of phase change materials (PCM) in Mobilized-Thermal Energy Storage (M-TES) for recovering low-temperature industrial waste heat (IWH) for distributed heat supply. *Renew. Energy* **2021**, *168*, 1040–1057. [CrossRef]
9. Regin, A.F.; Solanki, S.; Saini, J. Heat transfer characteristics of thermal energy storage system using PCM capsules: A review. *Renew. Sustain. Energy Rev.* **2008**, *12*, 2438–2458. [CrossRef]
10. da Cunha, J.P.; Eames, P. Thermal energy storage for low and medium temperature applications using phase change materials—A review. *Appl. Energy* **2016**, *177*, 227–238. [CrossRef]
11. Agyenim, F.; Hewitt, N.; Eames, P.; Smyth, M. A review of materials, heat transfer and phase change problem formulation for latent heat thermal energy storage systems (LHTESS). *Renew. Sustain. Energy Rev.* **2010**, *14*, 615–628. [CrossRef]
12. Youssef, Z.; Delahaye, A.; Huang, L.; Trinquet, F.; Fournaison, L.; Pollerberg, C.; Doetsch, C. State of the art on phase change material slurries. *Energy Convers. Manag.* **2013**, *65*, 120–132. [CrossRef]
13. Cristopia. Cristopia. Available online: <http://www.ciat.fr/rubrique/index/eng-product-ranges/33/CRISTOPIA/1509> (accessed on 20 September 2021).
14. Climator. Climator. 2016. Available online: <http://climator.com/> (accessed on 20 September 2021).
15. Rubitherm. Rubitherm. Available online: <http://www.rubitherm.eu> (accessed on 20 September 2021).
16. Microtek. Microtek. Available online: www.microteklabs.com (accessed on 20 September 2021).
17. Barreneche, C.; Navarro, M.E.; Cabeza, L.F.; Fernández, A.I. New database to select phase change materials: Chemical nature, properties, and applications. *J. Energy Storage* **2015**, *3*, 18–24. [CrossRef]
18. Sharma, A.; Tyagi, V.V.; Chen, C.R.; Buddhi, D. Review on thermal energy storage with phase change materials and applications. *Renew. Sustain. Energy Rev.* **2009**, *13*, 318–345. [CrossRef]
19. Sharma, S.D.; Kitano, H.; Sagara, K. Phase change materials for low temperature solar thermal applications. *Res. Rep. Fac. Eng. Mie Univ.* **2004**, *29*, 31–64.
20. Sharma, S.D.; Sagara, K. Latent Heat Storage Materials and Systems: A Review. *Int. J. Green Energy* **2005**, *2*, 1–56. [CrossRef]
21. Pandiyarajan, V.; Pandian, M.C.; Malan, E.; Velraj, R.; Seeniraj, R. Experimental investigation on heat recovery from diesel engine exhaust using finned shell and tube heat exchanger and thermal storage system. *Appl. Energy* **2011**, *88*, 77–87. [CrossRef]
22. Gasia, J.; Miró, L.; de Gracia, A.; Barreneche, C.; Cabeza, L. Experimental Evaluation of a Paraffin as Phase Change Material for Thermal Energy Storage in Laboratory Equipment and in a Shell-and-Tube Heat Exchanger. *Appl. Sci.* **2016**, *6*, 112. [CrossRef]
23. Ash, M. *Handbook of Textile Processing Chemicals*; Synapse Information Resources: Endicott, NY, USA, 2001.
24. Hale, D.V.H. *Phase Change Materials Handbook*. 1971. Available online: <https://ntrs.nasa.gov/search.jsp?R=19720012306> (accessed on 20 September 2021).
25. Kahwaji, S.; Johnson, M.B.; Kheirabadi, A.C.; Groulx, D.; White, M.A. Fatty acids and related phase change materials for reliable thermal energy storage at moderate temperatures. *Sol. Energy Mater. Sol. Cells* **2017**, *167*, 109–120. [CrossRef]
26. Lomonaco, A.; Haillot, D.; Pernot, E.; Franquet, E.; Bédécarrats, J.-P. Sodium nitrate thermal behavior in latent heat thermal energy storage: A study of the impact of sodium nitrite on melting temperature and enthalpy. *Sol. Energy Mater. Sol. Cells* **2016**, *149*, 81–87. [CrossRef]
27. Yuan, Y.; Zhang, N.; Li, T.; Cao, X.; Long, W. Thermal performance enhancement of palmitic-stearic acid by adding graphene nanoplatelets and expanded graphite for thermal energy storage: A comparative study. *Energy* **2016**, *97*, 488–497. [CrossRef]
28. Li, C.; Zhang, B.; Xie, B.; Zhao, X.; Chen, J.; Chen, Z.; Long, Y. Stearic acid/expanded graphite as a composite phase change thermal energy storage material for tankless solar water heater. *Sustain. Cities Soc.* **2018**, *44*, 458–464. [CrossRef]
29. Andiarito, R.; Nuryadin, M.K.; Taufik, A.; Saleh, R. Better latent heat and specific heat of stearic acid with magnetite/graphene nanocomposite addition for thermal storage application. *IOP Conf. Ser. Mater. Sci. Eng.* **2017**, *188*, 012049. [CrossRef]
30. Ferrer, G.; Barreneche, C.; Palacios, A.; Solé, A.; Fernández, A.I.; Cabeza, L.F. Empirical equations for viscosity and specific heat capacity determination of fatty acids. *J. Energy Storage* **2017**, *10*, 20–27. [CrossRef]
31. Regin, A.F.; Solanki, S.; Saini, J. An analysis of a packed bed latent heat thermal energy storage system using PCM capsules: Numerical investigation. *Renew. Energy* **2009**, *34*, 1765–1773. [CrossRef]

32. Verma, P.; Varun; Singal, S. Review of mathematical modeling on latent heat thermal energy storage systems using phase-change material. *Renew. Sustain. Energy Rev.* **2008**, *12*, 999–1031. [[CrossRef](#)]
33. Liu, S.; Li, Y.; Zhang, Y. Mathematical solutions and numerical models employed for the investigations of PCMs' phase transformations. *Renew. Sustain. Energy Rev.* **2014**, *33*, 659–674. [[CrossRef](#)]
34. Dutil, Y.; Rousse, D.R.; Salah, N.B.; Lassue, S.; Zalewski, L. A review on phase-change materials: Mathematical modeling and simulations. *Renew. Sustain. Energy Rev.* **2011**, *15*, 112–130. [[CrossRef](#)]
35. Al-Abidi, A.A.; Mat, S.B.; Sopian, K.; Sulaiman, M.Y.; Mohammed, A.T. CFD applications for latent heat thermal energy storage: A review. *Renew. Sustain. Energy Rev.* **2013**, *20*, 353–363. [[CrossRef](#)]
36. Ismail, K.A.R.; Henríquez, J.R. Numerical and experimental study of spherical capsules packed bed latent heat storage system. *Appl. Therm. Eng.* **2002**, *22*, 1705–1716. [[CrossRef](#)]
37. Bédécarrats, J.P.; Castaing-Lasvignottes, J.; Strub, F.; Dumas, J.P. Study of a phase change energy storage using spherical capsules. Part II: Numerical modelling. *Energy Convers. Manag.* **2009**, *50*, 2537–2546. [[CrossRef](#)]
38. Liao, Z.; Xu, C.; Ren, Y.; Gao, F.; Ju, X.; Du, X. A novel effective thermal conductivity correlation of the PCM melting in spherical PCM encapsulation for the packed bed TES system. *Appl. Therm. Eng.* **2018**, *135*, 116–122. [[CrossRef](#)]
39. Comini, G.; Del Giudice, S.; Lewis, R.W.; Zienkiewicz, O.C. Finite element solution of non-special reference to phase change. *Int. J. Numer. Methods Eng.* **1974**, *8*, 613–624. [[CrossRef](#)]
40. Gray, W.H.; Schnurr, N.M. A comparison of the finite element and finite difference methods for the analysis of steady two dimensional heat conduction problems. *Comput. Methods Appl. Mech. Eng.* **1975**, *6*, 243–245. [[CrossRef](#)]
41. Voller, V.R.; Cross, M.; Markatos, N.C. An enthalpy method for convection/diffusion phase change. *Int. J. Numer. Methods Eng.* **1987**, *24*, 271–284. [[CrossRef](#)]
42. Wen, C.; Sheffield, J.W.; O'Dell, M.P.; Leland, J.E. Analytical and experimental investigation of melting heat transfer. *J. Thermophys. Heat Transfer* **1989**, *3*, 330–339. [[CrossRef](#)]
43. Costa, M.; Buddhi, D.; Oliva, A. Numerical simulation of a latent heat thermal energy storage system with enhanced heat conduction. *Energy Convers. Manag.* **1998**, *39*, 319–330. [[CrossRef](#)]
44. de Gracia, A.; Cabeza, L.F. Numerical simulation of a PCM packed bed system: A review. *Renew. Sustain. Energy Rev.* **2017**, *69*, 1055–1063. [[CrossRef](#)]
45. König-Haagen, A.; Franquet, E.; Pernot, E.; Brüggemann, D. A comprehensive benchmark of fixed-grid methods for the modeling of melting. *Int. J. Therm. Sci.* **2017**, *118*, 69–103. [[CrossRef](#)]
46. Churchill, S.W.; Chu, H.H.S. Correlating equations for laminar and turbulent free convection from a vertical plate. *Int. J. Heat Mass Transf.* **1975**, *18*, 1323–1329. [[CrossRef](#)]
47. Franquet, E.; Gibout, S.; Bédécarrats, J.P.; Haillot, D.; Dumas, J.P. Inverse method for the identification of the enthalpy of phase change materials from calorimetry experiments. *Thermochim Acta* **2012**, *546*, 61–80. [[CrossRef](#)]
48. Li, T.; Lee, J.-H.; Wang, R.; Kang, Y.T. Heat transfer characteristics of phase change nanocomposite materials for thermal energy storage application. *Int. J. Heat Mass Transf.* **2014**, *75*, 1–11. [[CrossRef](#)]
49. Ma, G.; Sun, J.; Zhang, Y.; Jing, Y.; Jia, Y. Preparation and thermal properties of stearic acid-benzamide eutectic mixture/expanded graphite composites as phase change materials for thermal energy storage. *Powder Tech.* **2019**, *342*, 131–140. [[CrossRef](#)]
50. Karthikeyan, S.; Solomon, G.R.; Kumaresan, V.; Velraj, R. Parametric studies on packed bed storage unit filled with PCM encapsulated spherical containers for low temperature solar air heating applications. *Energy Convers. Manag.* **2014**, *78*, 74–80. [[CrossRef](#)]